

問1 (p5)

- (1) 単項式: ①, ③, ④ 多項式: ②, ⑤, ⑥
 (2) ① 2次式 ② 2次式 ③ 5次式
 ④ 2次式 ⑤ 2次式 ⑥ 1次式

問2

- (1) 項: $2x^2, -xy^2, 7xy, -9$
 係数: x^2 の係数 2, xy^2 の係数 -1, xy の係数 7
 次数: 3次式

$$(2) \frac{3xy - 4x^2 + 6xyz}{2}$$

$$= \frac{3xy}{2} - \frac{4x^2}{2} + \frac{6xyz}{2}$$

$$= \frac{3}{2}xy - 2x^2 + 3xyz$$

項: $\frac{3xy}{2}, -2x^2, 3xyz$

係数: xy の係数 $\frac{3}{2}$, x^2 の係数 -2, xyz の係数 3
 次数: 3次式

問3 (p7)

- (1) $2a + b + 7$ (2) $-2a - 3b - 2$
 (3) $-4x + 15y$ (4) $-5m - 5n + 11$

問4

- (1) (与式) = $3x - 2y + 7x + 5y = 10x + 3y$
 (2) (与式) = $3x - 6y - 7x - 5y = -4x - 11y$
 (3) (与式) = $8x - 2y - 5x + 10y = 3x + 8y$

問5

$(1) \begin{array}{r} 2x - 7y \\ +) 8x + 2y \\ \hline 10x - 5y \end{array}$	$(2) \begin{array}{r} a - 3b + 1 \\ -) 3a + 4b \\ \hline - 2a - 7b + 1 \end{array}$
$(3) \begin{array}{r} 7x - 9y + 13 \\ -) - 2x + y - 8 \\ \hline 9x - 10y + 21 \end{array}$	

演習1 (p8)

- (1) $6a + b$ (2) $a + 6$ (3) $7x - 2y$
 (4) $7a - 15b$ (5) $7x + 6y$ (6) $8x - 9y$
 (7) $8a + 7b$ (8) $8x - 9y$ (9) $3a - 6b$
 (10) $15a - 8b$

演習2 (p9)

- (1) $-8a + 5b + 3$
 (2) $8x - y$
 (3) $3x^2 - 2$
 (4) $x + \frac{1}{12}y$ ($= x + \frac{y}{12}$)
 (5) $\frac{1}{2}x - \frac{1}{2}y$ ($= \frac{x}{2} - \frac{y}{2}$ or $= \frac{x-y}{2}$)
 (6) $a - 4b$

演習3 (p11)

(2) 以降は、通常の計算の流れをお見せしました。

$$(1) \text{ (与式)} = \frac{3x}{6} - \frac{2(x-2y)}{6}$$

$$= \frac{3x - 2(x-2y)}{6}$$

$$= \frac{3x - 2x + 4y}{6}$$

$$= \frac{x + 4y}{6}$$

$$(2) \text{ (与式)} = \frac{5(x-2y) - 2(x+y)}{10}$$

$$= \frac{5x - 10y - 2x - 2y}{10}$$

$$= \frac{3x - 12y}{10}$$

$$(3) \text{ (与式)} = \frac{2(a+4b) - 3(3a-b)}{6}$$

$$= \frac{2a + 8b - 9a + 3b}{6}$$

$$= \frac{-7a + 11b}{6}$$

$$\begin{aligned}
 (4) \quad (\text{与式}) &= \frac{7a - 3b - 2(a + 2b)}{6} \\
 &= \frac{7a - 3b - 2a - 4b}{6} \\
 &= \frac{5a - 7b}{6}
 \end{aligned}$$

演習 4 (p12)

$$(1) \quad (\text{与式}) = \frac{7(x - y) - 2(x - 8y)}{14}$$

$$= \frac{7x - 7y - 2x + 16y}{14}$$

$$= \frac{5x + 9y}{14}$$

$$(2) \quad (\text{与式}) = \frac{3(2a + 3b) - 4(4a - 2b)}{12}$$

$$= \frac{6a + 9b - 16a + 8b}{12}$$

$$= \frac{-10a + 17b}{12}$$

$$(3) \quad (\text{与式}) = \frac{5(3x + y) - 2(4x - 2y)}{10}$$

$$= \frac{15x + 5y - 8x + 4y}{10}$$

$$= \frac{7x + 9y}{10}$$

$$(4) \quad (\text{与式}) = \frac{-3(x - 7y) - 2(4x - y)}{6}$$

$$= \frac{-3x + 21y - 8x + 2y}{6}$$

$$= \frac{-11x + 23y}{6}$$

演習 5 (p13)

(1) (2) で違う計算方法をお見せします。(3) 以降は (2) の方法で表します。

$$(1) \quad (\text{与式}) = \frac{1}{6} \{2(2x + 5) - (4x + 3)\}$$

$$= \frac{1}{6} (4x + 10 - 4x - 3)$$

$$= \frac{1}{6} \times 7 = \frac{7}{6}$$

$$\begin{aligned}
 (2) \quad (\text{与式}) &= \frac{3(x - 3y) - 2(2x - 3y)}{12} \\
 &= \frac{3x - 9y - 4x + 6y}{12} \\
 &= \frac{-x - 3y}{12} \left(= -\frac{x + 3y}{12}\right)
 \end{aligned}$$

$$(3) \quad (\text{与式}) = \frac{7(x - 3) - 2(3x - 8)}{14}$$

$$= \frac{7x - 21 - 6x + 16}{14}$$

$$= \frac{x - 5}{14}$$

$$(4) \quad (\text{与式}) = \frac{3(2x + 3) - 5(x + 2)}{15}$$

$$= \frac{6x + 9 - 5x - 10}{15}$$

$$= \frac{x - 1}{15}$$

演習 6 (p14)

$$\begin{aligned}
 (1) \quad (\text{与式}) &= \frac{3(a + 2b) - (2a + 5b)}{3} \\
 &= \frac{3a + 6b - 2a - 5b}{3} \\
 &= \frac{a + b}{3}
 \end{aligned}$$

$$(2) \quad (\text{与式}) = a + 2b - 3a + 3b = -2a + 5b$$

$$(3) \quad (\text{与式}) = \frac{5(x - y) - (x - 2y)}{5}$$

$$= \frac{5x - 5y - x + 2y}{5}$$

$$= \frac{4x - 3y}{5}$$

$$(4) \quad (\text{与式}) = \frac{2(x - y) + (x + 3y)}{2}$$

$$= \frac{2x - 2y + x + 3y}{2}$$

$$= \frac{3x + y}{2}$$

演習 7 (p15)

$$(1) \quad (\text{与式}) = 2(x - 2y) - 3(x - 3y)$$

$$= 2x - 4y - 3x + 9y$$

$$= -x + 5y$$

$$\begin{aligned}
 (2) \quad (\text{与式}) &= \frac{2 \times 2x - 6y - 3(x - 2y)}{6} \\
 &= \frac{4x - 6y - 3x + 6y}{6} \\
 &= \frac{x}{6} \left(= \frac{1}{6}x\right)
 \end{aligned}$$

$$(3) \quad (\text{与式}) = \frac{5(x - 2y) - 3(6x - y) + 15x}{15}$$

$$= \frac{5x - 10y - 18x + 3y + 15x}{15}$$

$$= \frac{2x - 7y}{15}$$

$$(4) \quad (\text{与式}) = \frac{3(3x + y) + (5x - y) - 2(4x - 2y)}{6}$$

$$= \frac{9x + 3y + 5x - y - 8x + 4y}{6}$$

$$= \frac{6x + 6y}{6} = x + y$$

演習 8 (p17)

$$\begin{array}{lll}
 (1) \quad 8a^2b & (2) \quad 15x^2y & (3) \quad -54x^3y^2 \\
 (4) \quad \frac{1}{3}a^3b & (5) \quad 2xy^2 & (6) \quad -2ab^3 \\
 (7) \quad 3x^5y^2 & (8) \quad 5ab^4 & (9) \quad 2x^3y \\
 (10) \quad \frac{27}{8}x^2y^2 & &
 \end{array}$$

演習 9

$$\begin{array}{ll}
 (1) \quad 54a^3b & (2) \quad 8a^3 \\
 (3) \quad 6a^3b & (4) \quad -18a^3b^4
 \end{array}$$

演習 10 (p18)

$$(1) \quad (\text{与式}) = \frac{6 \times x \times y}{3 \times x} = 2y$$

$$(2) \quad (\text{与式}) = \frac{14 \times a \times a \times b}{2 \times a} = 7ab$$

$$(3) \quad (\text{与式}) = \frac{8 \times a \times b \times b}{-4 \times b} = -2ab$$

$$(4) \quad (\text{与式}) = \frac{10 \times x \times x \times x \times y \times y}{5 \times x \times y} = 2x^2y$$

$$(5) \quad (\text{与式}) = \frac{8 \times x \times y \times y}{2 \times x \times y} = 4y$$

$$(6) \quad (\text{与式}) = \frac{7 \times x \times x \times x \times y \times y}{x \times y} = 7x^2y$$

$$(7) \quad (\text{与式}) = \frac{6 \times a \times b \times b}{3 \times a \times b} = 2b$$

$$(8) \quad (\text{与式}) = \frac{27 \times a \times a \times b}{-9 \times a \times b} = -3a$$

演習 11 (p19)

$$(1) \quad (\text{与式}) = -3x^{2-1} \times 1 = -3x$$

$$(2) \quad (\text{与式}) = -3a^{2-1} \times 1 = -3a$$

$$(3) \quad (\text{与式}) = \frac{-2b^{2-1}}{a^{2-1}} = -\frac{2b}{a}$$

$$(4) \quad (\text{与式}) = 7a^{3-2}b^{3-1} = 7ab^2$$

$$(5) \quad (\text{与式}) = -\frac{6}{4}a^{2-1} = -\frac{3}{2}a$$

$$(6) \quad (\text{与式}) = \frac{2}{12}a^{3-2} \times 1 = \frac{1}{6}a$$

$$(7) \quad (\text{与式}) = 12a^2b^2 \div 4a^2 = 3 \times 1 \times b^2 = 3b^2$$

$$(8) \quad (\text{与式}) = 18x^2y^3 \div 9y^2 = 2x^2y^{3-2} = 2x^2y$$

演習 12 (p20)

$$(1) \quad (\text{与式}) = 4xy \times \frac{3}{2x} = 2y \times 3 = 6y$$

$$(2) \quad (\text{与式}) = -6xy^2 \times \frac{3}{xy} = -6y \times 3 = -18y$$

$$(3) \quad (\text{与式}) = \frac{8}{3}x^3y^4 \times \frac{9}{2x^2y}$$

$$= \frac{4}{1}x^{3-2}y^{4-1} \times \frac{3}{1} = 12xy^3$$

$$(4) \quad (\text{与式}) = \frac{18}{5}x^2y \times \frac{10}{9x} = \frac{2}{1}x^{2-1}y \times \frac{2}{1} = 4xy$$

演習 13 (p21)

$$(1) \quad (\text{与式}) = 20x^3y \times \frac{1}{5x} \times \frac{1}{2y}$$

$$= 20x^3y \times \frac{1}{10xy}$$

$$= 2x^{3-1} \times 1 = 2x^2$$

$$(2) \quad (\text{与式}) = 30ab^2 \times \frac{1}{3b} \times \frac{1}{5ab}$$

$$= 30ab^2 \times \frac{1}{15ab^2}$$

$$= 2 \times 1 \times 1 = 2$$

$$(3) \text{ (与式)} = -8x^5y^4 \times \left(-\frac{3}{2x^3y}\right) \times \left(-\frac{5}{12xy^3}\right)$$

$$= -8x^5y^4 \times \frac{15}{24x^4y^4}$$

$$= -\frac{15}{3} x^{5-4} \times 1 = -5x$$

演習 14

$$\begin{array}{ll} (1) & 3a - 8 \\ (2) & 3a - 2 \\ (3) & 9ab - 1 \\ (4) & 2a - 5b \\ (5) & 2a - 7b \\ (6) & 4a - 3 \\ (7) & xy - 2 \\ (8) & -3x + 2y \\ (9) & 1 - 2b \\ (10) & xy + 2 \end{array}$$

演習 15 (p23)

$$\begin{array}{l} (1) \text{ (与式)} = 24x^2y \div 3x = 8xy \\ (2) \text{ (与式)} = \frac{1}{3} a \times 9b = 3ab \\ (3) \text{ (与式)} = a^3b^4 \div ab^3 = a^2b \\ (4) \text{ (与式)} = 5ab \times 5a = 25a^2b \\ (5) \text{ (与式)} = 24x^3y^2 \div 8xy = 3x^2y \\ (6) \text{ (与式)} = \frac{9}{4} b \times 4ab = 9ab^2 \\ (7) \text{ (与式)} = 12x^3y^2 \div 2xy = 6x^2y \\ (8) \text{ (与式)} = -\frac{5a}{3b} \times 3ab = -5a^2 \\ (9) \text{ (与式)} = -12a^2b^2 \div 6ab = -2ab \\ (10) \text{ (与式)} = -\frac{1}{2} xy \times (-6x) = 3x^2y \\ (11) \text{ (与式)} = 24a^3b^3 \div 2a = 12a^2b^3 \end{array}$$

演習 16 (p24)

$$\begin{array}{l} (1) \text{ (与式)} = 12a^3b^2 \div 6ab^2 = 2a^2 \\ (2) \text{ (与式)} = -3b \times (-a^2) = 3a^2b \\ (3) \text{ (与式)} = 8x^3y \div (-2x) = -4x^2y \\ (4) \text{ (与式)} = -\frac{5}{2} ab^2 \times (-6ab) = 15a^2b^3 \\ (5) \text{ (与式)} = \frac{3}{4a} b^2 \times 3ab = \frac{9}{4} b^3 \\ (6) \text{ (与式)} = -\frac{3}{4b^2} \times 6ab^2 = -\frac{9}{2} a \\ (7) \text{ (与式)} = 2a^2b \div 4ab^2 = \frac{2a^2b}{4ab^2} = \frac{a}{2b} \end{array}$$

$$(8) \text{ (与式)} = -\frac{16}{10} xy \times \left(-\frac{35}{10} x\right) \div \frac{2}{10} y$$

$$= \frac{8}{5} xy \times \frac{7}{2} x \times \frac{10}{2y}$$

$$= \frac{8 \times 7 \times 10}{5 \times 2 \times 2} x^2 = 28x^2$$

演習 17 (p25)

$$(1) \text{ (与式)} = -\frac{a^2}{3b} \times \frac{a}{b} = -\frac{a^3}{3b^2}$$

$$(2) \text{ (与式)} = -2a^3b^2 \times \left(-\frac{10}{9} \times \frac{1}{a^2b}\right) \times \frac{3}{8} ab^2$$

$$= 2 \times \frac{10}{9} \times \frac{3}{8} \times a^3b^2 \times \frac{1}{a^2b} \times ab^2$$

$$= \frac{5}{6} a^2b^3$$

$$(3) \text{ (与式)} = \frac{8}{5} x^3 \times \left(-\frac{15}{4} \times \frac{1}{x^2y}\right) \times xy$$

$$= -\frac{8}{5} \times \frac{15}{4} \times x^3 \times \frac{1}{x^2y} \times xy$$

$$= -6x^2$$

$$(4) \text{ (与式)} = 6a^2 \times \left(-\frac{1}{2} ab^2\right) \times \frac{1}{9} \times \frac{1}{ab}$$

$$= -6 \times \frac{1}{2} \times \frac{1}{9} \times a^2 \times ab^2 \times \frac{1}{ab}$$

$$= -\frac{1}{3} a^2b$$

$$(5) \text{ (与式)} = 12ab^2 \times \frac{15}{4} \times \frac{1}{ab} \times \frac{5}{9} a$$

$$= 12 \times \frac{15}{4} \times \frac{5}{9} \times ab^2 \times \frac{1}{ab} \times a$$

$$= 25ab$$

演習 18 (p26)

$$(1) \text{ (与式)} = 4a^2 \div 2ab \times 3b^3$$

$$= 4 \times \frac{1}{2} \times 3 \times a^2 \times \frac{1}{ab} \times b^3$$

$$= 6ab^2$$

$$(2) \text{ (与式)} = 18xy \times x^2y \div 9x^2$$

$$= 18 \times \frac{1}{9} \times xy \times x^2y \times \frac{1}{x^2}$$

$$= 2xy^2$$

$$(3) \text{ (与式)} = 2a^3b \div 16a^2b^2 \times (-4b)$$

$$= 2 \times \frac{1}{16} \times (-4) \times a^3b \times \frac{1}{a^2b^2} \times b$$

$$= -\frac{1}{2} a$$

$$(4) \text{ (与式)} = 9a^2 \times 4b \div (-6ab)$$

$$= 9 \times 4 \times \left(-\frac{1}{6}\right) \times a^2 \times b \times \frac{1}{ab}$$

$$= -6a$$

$$(5) \text{ (与式)} = 18a^2b \div 9b^2 \times (-ab^3)$$

$$= -18 \times \frac{1}{9} \times a^2b \times \frac{1}{b^2} \times ab^3$$

$$(6) \text{ (与式)} = -8 \times a^2b^3 \times \frac{1}{4} \times \frac{1}{ab^2}$$

$$= -8 \times \frac{1}{4} \times a^2b^3 \times \frac{1}{ab^2}$$

$$= -2ab$$

$$(7) \text{ (与式)} = 8x^3y \div 4x^2y^2 \times 5y$$

$$= 8 \times \frac{1}{4} \times 5 \times x^3y \times \frac{1}{x^2y^2} \times y$$

$$= 10x$$

$$(8) \text{ (与式)} = 4a^2b^2 \times 3a^2b \times \frac{1}{4} \times \frac{1}{ab^2}$$

$$= 4 \times 3 \times \frac{1}{4} \times a^2b^2 \times a^2b \times \frac{1}{ab^2}$$

$$= 3a^3b$$

演習 19 (p27)

$$(1) \text{ (与式)} = -\frac{10}{3} a \times \frac{9}{25} b^2 = -\frac{6}{5} ab^2$$

$$(2) \text{ (与式)} = 36a^3b \div 9a^2b^4 \times \left(-\frac{1}{2} ab^4\right)$$

$$= 36 \times \frac{1}{9} \times \left(-\frac{1}{2}\right) \times a^3b \times \frac{1}{a^2b^4} \times ab^4$$

$$= -2a^2b$$

$$(3) \text{ (与式)} = 36a^2b^2 \times \frac{2}{3} \times \frac{1}{ab^2} \times \left(-\frac{1}{27}\right)$$

$$= 36 \times \frac{2}{3} \times \left(-\frac{1}{27}\right) \times a^2b^2 \times \frac{1}{ab^2}$$

$$= -\frac{8}{9} a$$

$$(4) \text{ (与式)} = 2a + 6a = 8a$$

$$(5) \text{ (与式)} = 4a - \frac{4}{3} - 4a = -\frac{4}{3}$$

$$(6) \text{ (与式)} = 2a - 6 + 4b + 6 - 4b = 2a$$

演習 20 (p28)

$$(1) \text{ (与式)} = \frac{24}{(-2)^2} = \frac{24}{4} = 6$$

$$(2) \text{ (与式)} = (-2)^2 + 2 \times (-2) \times 4$$

$$= 4 - 16 = -12$$

$$(3) \text{ (与式)} = \frac{2}{3} - 2 \times \frac{1}{4}$$

$$= \frac{2}{3} - \frac{1}{2}$$

$$= \frac{4}{6} - \frac{3}{6} = \frac{1}{6}$$

$$(4) \text{ (与式)} = 3 \times 2^2 - 2 \times (-3)$$

$$= 3 \times 4 + 6$$

$$= 12 + 6 = 18$$

演習 21 (p29)

$$(1) \text{ (与式)} = 10a - 4b - 9a + 3b$$

$$= a - b$$

$$= -2 - 3 = -5$$

$$(2) \text{ (与式)} = \frac{1}{2} xy \times 6x$$

$$= 3x^2y$$

$$= 3 \times (-2)^2 \times 5$$

$$= 3 \times 4 \times 5 = 60$$

$$(3) \text{ (与式)} = \frac{3(3a - 4b) - 2(2a - b)}{6}$$

$$= \frac{9a - 12b - 4a + 2b}{6}$$

$$= \frac{5a - 10b}{6}$$

$$= \frac{5(a - 2b)}{6}$$

$$= \frac{5 \times 3}{6} = \frac{5}{2}$$

演習 22

$$\frac{11}{7} = 1.571\cdots \text{ より, } a = 5, b = 7, c = 1$$

$$\begin{aligned} \text{よって, } 100a + 10b + c &= 100 \times 5 + 10 \times 7 + 1 \\ &= 500 + 70 + 1 = 571 \end{aligned}$$

演習 23 (p31)

$$(1) 3a - 2b = 8$$

$$\begin{aligned} -2b &= 8 - 3a \\ b &= \frac{8 - 3a}{-2} \quad \left[= -\frac{1}{2}(8 - 3a) \right] \\ &= \frac{3a - 8}{2} \quad \left[= \frac{1}{2}(3a - 8) \right] \text{ (答)} \end{aligned}$$

$$(2) x - 4y - 12 = 0$$

$$\begin{aligned} -4y &= -x + 12 \\ y &= \frac{-x + 12}{-4} \quad \left[= -\frac{1}{4}(-x + 12) \right] \\ &= \frac{x - 12}{4} \quad \left[= \frac{1}{4}(x - 12) \right] \text{ (答)} \end{aligned}$$

(3) (1)(2)の2行目でマイナスの数で両辺をわるのが嫌なので、別の流れをお見せします。

$$\begin{aligned} 2x - 7y &= 5 \rightarrow -7y \text{ を右辺, 5を左辺に移} \\ &\text{行し, 両辺をひっくり返す。} \\ 7y &= 2x - 5 \\ y &= \frac{2x - 5}{7} \quad \left[= \frac{1}{7}(2x - 5) \right] \text{ (答)} \end{aligned}$$

(4) 【多くの人の流れ】

$$\ell = 2(a + b)$$

$$= 2a + 2b$$

$$-2a = 2b - \ell$$

$$a = \frac{-2b + \ell}{2} \quad \left(\text{答} \right)$$

【お薦めの流れ】

$$\ell = 2(a + b)$$

$$2(a + b) = \ell$$

$$a + b = \frac{\ell}{2}$$

$$a = \frac{\ell}{2} - b \quad \left(\text{答} \right)$$

$$\begin{aligned} (5) 4x - \frac{1}{2}y &= 6 \rightarrow -\frac{1}{2}y \text{ を右辺, 6を左辺に移} \\ &\text{行し, 両辺をひっくり返す。} \end{aligned}$$

$$\frac{1}{2}y = 4x - 6 \quad \leftarrow$$

$$y = 8x - 12 \quad \left(\text{答} \right)$$

$$(6) a + \frac{b}{3} = 2c$$

$$\frac{b}{3} = 2c - a$$

$$b = 6c - 3a \quad \left(\text{答} \right)$$

$$(7) V = \frac{1}{3} Sh$$

$$\frac{S}{3} h = V$$

$$h = V \times \frac{3}{S}$$

$$= \frac{3V}{S} \quad \left(\text{答} \right)$$

演習 24 (p32)

$$(1) b = \frac{a - 1}{4}$$

$$4b = a - 1$$

$$a = 4b + 1 \quad \left(\text{答} \right)$$

$$(2) a = \frac{5b + 3c}{8}$$

$$8a = 5b + 3c$$

$$3c = 8a - 5b$$

$$c = \frac{8a - 5b}{3} \quad \left(\text{答} \right)$$

$$(3) c = \frac{10a - b}{9}$$

$$9c = 10a - b$$

$$b = 10a - 9c \quad \left(\text{答} \right)$$

$$(4) m = \frac{a + 3b}{4}$$

$$4m = a + 3b$$

$$3b = 4m - a$$

$$b = \frac{4m - a}{3} \quad \left(\text{答} \right)$$

$$(5) b = \frac{3a + 1}{2}$$

$$2b = 3a + 1$$

$$3a = 2b - 1$$

$$a = \frac{2b - 1}{3} \quad \left(\text{答} \right)$$

$$(6) a = \frac{b + 2c}{3}$$

$$3a = b + 2c$$

$$2c = 3a - b$$

$$c = \frac{3a - b}{2} \quad \left(\text{答} \right)$$

$$(7) m = \frac{2a + b + c}{4}$$

$$4m = 2a + b + c$$

$$c = 4m - 2a - b \quad \left(\text{答} \right)$$

演習 25 (p33)

$$a = 7 \times b + 3 = 7b + 3$$

$$\text{だから, } 7b = a - 3 \quad b = \frac{a - 3}{7} \quad \text{よって, 工 (答)}$$

演習 26

$$y = \frac{1}{2}x + 3$$

$$2y = x + 6$$

$$\text{だから, } x - 2y + 6 = 0$$

よって, 6 (答)

演習 27 (p35)

$$(1) p \div 3 = m \text{ あまり } 2 \text{ より, } p = 3m + 2$$

$$\text{よって, } m = \frac{p - 2}{3} \quad \left(\text{答} \right)$$

$$(2) b = a - \frac{a}{10} \times p = a - \frac{ap}{10} \quad \left[= a \left(1 - \frac{p}{10} \right) \right]$$

$$\text{よって, } b = a - \frac{ap}{10} \quad \left[= a \left(1 - \frac{p}{10} \right) \right] \quad \left(\text{答} \right)$$

$$(3) \text{ 全生徒数を } x \text{ とおくと, 中学1年生は } \frac{1}{3}x \text{ であり,}$$

$$\text{中学1年生が } a \text{ 人より, } \frac{1}{3}x = a$$

だから, 全生徒数は $x = 3a \cdots ①$ と表せる。

また, 2年生が b 人なので①より,

3年生の人数は, $3a - a - b = 2a - b$ 人。

そこで, 条件より, $b : (2a - b) = 5 : 6$ ゆえ,

$$6b = 5(2a - b) \quad 6b = 10a - 5b \quad 11b = 10a$$

$$b = \frac{10}{11}a \quad \text{よって, } b = \frac{10}{11}a \quad \left(\text{答} \right)$$

$$(4) A = 3m + 2, B = 3n + 2 \text{ より,}$$

$$A + B = (3m + 2) + (3n + 2)$$

$$= 3m + 2 + 3n + 2$$

$$= 3m + 3n + 4$$

$$= 3m + 3n + 3 + 1$$

$$= 3(m + n + 1) + 1 \cdots (*)$$

$m + n + 1$ は整数ゆえ, $3(m + n + 1)$ は3の倍数。

よって, (*)より, 商は $m + n + 1$, 余りは 1 (答)

(5) B の底面の半径を r とおくと, A の底面の半径は $2r$ となる。また, 高さを h とする。

A の体積は, $(2r)^2 \times \pi \times h = 4\pi r^2 h \cdots ①$

B の体積は, $r^2 \times \pi \times h \times \frac{1}{3} = \frac{1}{3}\pi r^2 h \cdots ②$

① ÷ ② より,

$$4\pi r^2 h \div \frac{1}{3}\pi r^2 h = 4 \times \frac{3}{1} = 12 \quad \text{よって, 12倍 (答)}$$

問 6 (p37)

(1) [証明]

2つの偶数を $2m, 2n$ とおくと,

$$2m + 2n = 2(m + n)$$

ここで, $(m + n)$ は整数なので, $2(m + n)$ は2の倍数である。

よって, 偶数と偶数の和は, 偶数である。

おわり

(2) [証明]

奇数を $2m + 1$, 偶数を $2n$ とおくと,

$$(2m + 1) + 2n = 2m + 1 + 2n$$

$$= 2(m + n) + 1$$

ここで, $(m + n)$ は整数なので, $2(m + n)$ は偶数ゆえ, $2(m + n) + 1$ は奇数である。

よって, 奇数と偶数の和は, 奇数である。

おわり

問 7

(1) [証明]

2つの奇数を $2m + 1, 2n - 1$ とおくと,

$$(2m + 1) + (2n - 1) = 2m + 1 + 2n - 1$$

$$= 2m + 2n$$

$$= 2(m + n)$$

ここで, $(m + n)$ は整数なので, $2(m + n)$ は2の倍数である。

よって, 奇数と奇数の和は, 偶数である。

おわり

(2) [証明]

奇数を $2m + 1$, 偶数を $2n$ とおくと,

$$(2m + 1) \times 2n = 4mn + 2n$$

$$= 2(2mn + n)$$

ここで, $(2mn + n)$ は整数なので, $2(2mn + n)$ は偶数である。

よって, 奇数と偶数の積は, 偶数である。

おわり